

Calculus Warm Up #10-2

use L'Hôpital's Rule to evaluate (k is a constant $\neq 0$)

$$1. \lim_{x \rightarrow k} \frac{\sqrt[3]{x} - \sqrt[3]{k}}{x - k}$$

$$2. \lim_{x \rightarrow 1^+} \left(\frac{2}{\ln x} - \frac{2}{x - 1} \right)$$

HW Questions:

In Exercises 1–4, evaluate the limit (a) using techniques from Chapters 2 and 4 and (b) using L'Hôpital's Rule.

$$1. \lim_{x \rightarrow 3} \frac{2(x - 3)}{x^2 - 9}$$

$$3. \lim_{x \rightarrow \infty} \frac{5x^2 - 3x + 1}{3x^2 - 5}$$

In Exercises 5–30, evaluate each limit, using L'Hôpital's Rule if necessary.

$$5. \lim_{x \rightarrow 2} \frac{x^2 - x - 2}{x - 2}$$

$$7. \lim_{x \rightarrow 0} \frac{\sqrt{4 - x^2} - 2}{x}$$

$$9. \lim_{x \rightarrow 0} \frac{e^x - (1 - x)}{x}$$

In Exercises 5–30, evaluate each limit, using L'Hôpital's Rule if necessary.

11. $\lim_{x \rightarrow 0^+} \frac{e^x - (1+x)}{x^n}, \quad n = 1, 2, 3, \dots$

if $n=1 \rightarrow 0$
 $n=2 \rightarrow \frac{1}{2}$
 $n=3 \rightarrow$

$n=4 \rightarrow \lim_{x \rightarrow 0} \frac{e^x - (1+x)}{x^4}$

$\frac{e^x - 1}{4x^3} \rightarrow \frac{e^x}{12x^2}$

$\frac{1}{0} \rightarrow \infty$

13. $\lim_{x \rightarrow \infty} \frac{\ln x}{x}$

15. $\lim_{x \rightarrow \infty} \frac{3x^2 - 2x + 1}{2x^2 + 3}$

for $n \geq 3$

∞

17. $\lim_{x \rightarrow \infty} \frac{x^2 + 2x + 3}{x - 1}$

19. $\lim_{x \rightarrow 0^+} [x^2 \ln x]$

21. $\lim_{x \rightarrow 2} \left(\frac{8}{x^2 - 4} - \frac{x}{x - 2} \right)$

$\lim_{x \rightarrow 0^+} \frac{\ln x}{x^{-2}}$

$\frac{\frac{1}{x}}{-2x^{-3}} \rightarrow \frac{x^3}{-2x^2}$

$\lim_{x \rightarrow 0^+} \left(\frac{x^2}{-2} \right)$

0

$$23. \lim_{x \rightarrow \infty} \frac{x}{\sqrt{x^2 + 1}}$$

$$25. \lim_{x \rightarrow 0^+} x^{1/x}$$

$$27. \lim_{x \rightarrow \infty} x^{1/x}$$

$$29. \lim_{x \rightarrow \infty} (1 + x)^{1/x}$$

$$\text{let } \sqrt{x^2} = x$$

$$\lim_{x \rightarrow \infty} \frac{\frac{x}{x}}{\sqrt{\frac{x^2}{x^2} + \frac{1}{x}}}$$

$$\lim_{x \rightarrow \infty} \frac{1}{\sqrt{1 + \frac{1}{x}}}$$

$$\lim_{x \rightarrow \infty} \frac{1}{\frac{1}{2}(x^2+1)^{1/2}(\frac{1}{2}x)}$$

$$\lim_{x \rightarrow \infty} \frac{\frac{1}{x}}{\frac{\sqrt{x^2+1}}{x}}$$

$$\frac{\infty}{\infty}$$

$$\frac{\infty}{\infty}$$

$$23. \lim_{x \rightarrow \infty} \frac{x}{\sqrt{x^2 + 1}}$$

$$25. \lim_{x \rightarrow 0^+} x^{1/x}$$

$$27. \lim_{x \rightarrow \infty} x^{1/x}$$

$$29. \lim_{x \rightarrow \infty} (1 + x)^{1/x}$$

$$0^{\frac{1}{0}} = 0^{\infty} = 0$$

$$\infty^{\frac{1}{0}} = \infty^0 = 0$$

$$\lim_{x \rightarrow \infty} \frac{1}{x} \ln x = \frac{\infty}{\infty}$$

$$\lim_{x \rightarrow \infty} \frac{1}{x} = \frac{1}{\infty} = 0$$

$$\boxed{\ln y} = 0$$

$$e^0 = y$$

$$= 1$$

Summary:

Indeterminate Forms

0^0

∞^0

1^∞

Use Natural Logarithms

$\frac{0}{0}$

$\frac{\infty}{\infty}$

Use L'Hôpital's Rule

$\infty - \infty$

Change the form by adding or subtracting

$0 \cdot \infty$

Change the form to get $\frac{0}{0}$ or $\frac{\infty}{\infty}$ and then use L'Hôpital's Rule

Determinate Forms

$\infty + \infty = \infty$

$-\infty - \infty = -\infty$

$0^\infty = 0$

$\frac{1}{0^\infty}$

$\leftarrow 0^{-\infty} = \infty$

$\frac{0}{L}$

$\frac{L}{\pm\infty}$

$\frac{0}{\pm\infty}$

Limit is Zero

$\frac{L}{0}$

$\frac{\pm\infty}{L}$

$\frac{\pm\infty}{0}$

Limit is Infinite

Classwork: Rev. #1 (Green)

Next test is Monday, Nov. 13

Covers: 7.2, 7.5 & 7.8

and past topics:

evaluate limits, continuity, concavity,
instantaneous rate of change, implicit
differentiation

HW: p. 415

13 - 37 odd, 85 - 91 odd